

8-3 Slope of a Line

Objective: To find the slope of a line.

Vocabulary

Slope If (x_1, y_1) and (x_2, y_2) are *any* two different points on a line,

$$\text{Slope} = \frac{\text{rise}}{\text{run}} = \frac{\text{difference between } y\text{-coordinates}}{\text{difference between } x\text{-coordinates}} = \frac{y_2 - y_1}{x_2 - x_1}$$

Positive slope The slope of a line that rises from left to right is positive.

Negative slope The slope of a line that falls from left to right is negative.

Zero slope A horizontal line has slope 0.

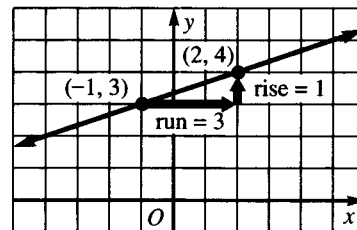
No slope A vertical line has no slope.

Collinear points Points that lie on the same line.

Example 1 Find the slope of the line through $(-1, 3)$ and $(2, 4)$.

Solution Let $(x_1, y_1) = (-1, 3)$ and $(x_2, y_2) = (2, 4)$.

$$\text{Slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4 - 3}{2 - (-1)} = \frac{1}{3}$$



Example 2 Find the slope of the line through $(1, -3)$ and $(4, -3)$.

Solution Slope = $\frac{-3 - (-3)}{4 - 1} = \frac{0}{3} = 0$ The line has slope 0.

Example 3 Find the slope of the line through $(2, -1)$ and $(2, 5)$.

Solution Slope = $\frac{5 - (-1)}{2 - 2} = \frac{6}{0}$ (undefined) The line has *no* slope.

Find the slope of the line through the given points.

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|------------------------|------------------------|-----------------------|
| 1. $(5, -6), (2, -4)$ | 2. $(-3, 6), (-5, 4)$ | 3. $(0, 1), (2, -2)$ |
| 4. $(1, 2), (4, 6)$ | 5. $(2, 1), (8, -2)$ | 6. $(-1, 5), (0, 0)$ |
| 7. $(4, 3), (2, 7)$ | 8. $(5, 2), (-1, 2)$ | 9. $(-3, -4), (1, 2)$ |
| 10. $(-5, 2), (7, -6)$ | 11. $(1, 4), (-3, 0)$ | 12. $(4, 4), (-4, 6)$ |
| 13. $(8, -1), (6, 0)$ | 14. $(3, -1), (-2, 4)$ | 15. $(7, 4), (7, -4)$ |

8-3 Slope of a Line (continued)**Example 4** Find the slope of the line with the equation $2x + 3y = 6$.**Solution** 1. First find any two points on the line.

$$\begin{array}{ll} \text{If } x = 0: & 2(0) + 3y = 6 \\ & 3y = 6 \\ & y = 2 \\ \text{One point:} & (0,2) \end{array} \qquad \begin{array}{ll} \text{If } y = 0: & 2x + 3(0) = 6 \\ & 2x = 6 \\ & x = 3 \\ \text{Another point:} & (3,0) \end{array}$$

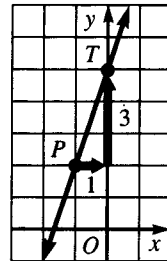
$$2. \text{ Now use the slope formula. Slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - 2}{3 - 0} = -\frac{2}{3}$$

Find the slope of each line. If the line has no slope, say so.

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|-------------------|--------------------|--------------------|------------------|
| 16. $y = 2x - 1$ | 17. $y = 3x + 2$ | 18. $y = 4 - 2x$ | 19. $y = 6 - 3x$ |
| 20. $6x + 2y = 3$ | 21. $2x - 5y = 10$ | 22. $3x + 6y = 12$ | 23. $x - 2y = 4$ |
| 24. $y = 5$ | 25. $y + 2 = 0$ | 26. $x = 1$ | 27. $2x - 3 = 0$ |

Example 5 Draw a line through the point $P(-1, 2)$ with a slope of 3.

- Solution**
- Plot point P .
 - Write the slope as $\frac{3}{1}$. Rise = 3. Run = 1.
 - From P , measure 1 unit to the right and 3 units up to locate a second point, T .
 - Draw the line through P and T .

**Through the given point, draw a line with the given slope.**

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|---------------------------------------|---------------------------------------|--------------------------------------|
| 28. $A(2, 1)$; slope 2 | 29. $B(-2, 3)$; slope -3 | 30. $C(1, -4)$; slope 4 |
| 31. $D(-3, -2)$; slope $\frac{2}{3}$ | 32. $E(-4, 1)$; slope $-\frac{1}{2}$ | 33. $F(3, 0)$; slope $-\frac{3}{4}$ |
| 34. $G(-2, -1)$; slope $\frac{2}{5}$ | 35. $H(-5, 2)$; slope -2 | 36. $I(2, -3)$; slope -1 |

Mixed Review Exercises

Solve.

$$1. \frac{x+2}{2} + \frac{x}{4} = 0 \qquad 2. -3 = \frac{9b}{4} \qquad 3. \frac{2+z}{3z} = \frac{4}{z} \qquad 4. -3(y+2) = 9$$

Evaluate if $x = -2$, $y = 1$, $a = 3$, and $b = -4$.

$$5. \frac{a+2b}{2a-b} \qquad 6. 3(x+3y) \qquad 7. \frac{1}{2}(3x+4y) \qquad 8. (2a-3b)+5$$